

Tracer Budgets in ECCO—Part I: Overview and Some Applications

Christopher G. Piecuch (cpiecuch@whoi.edu)

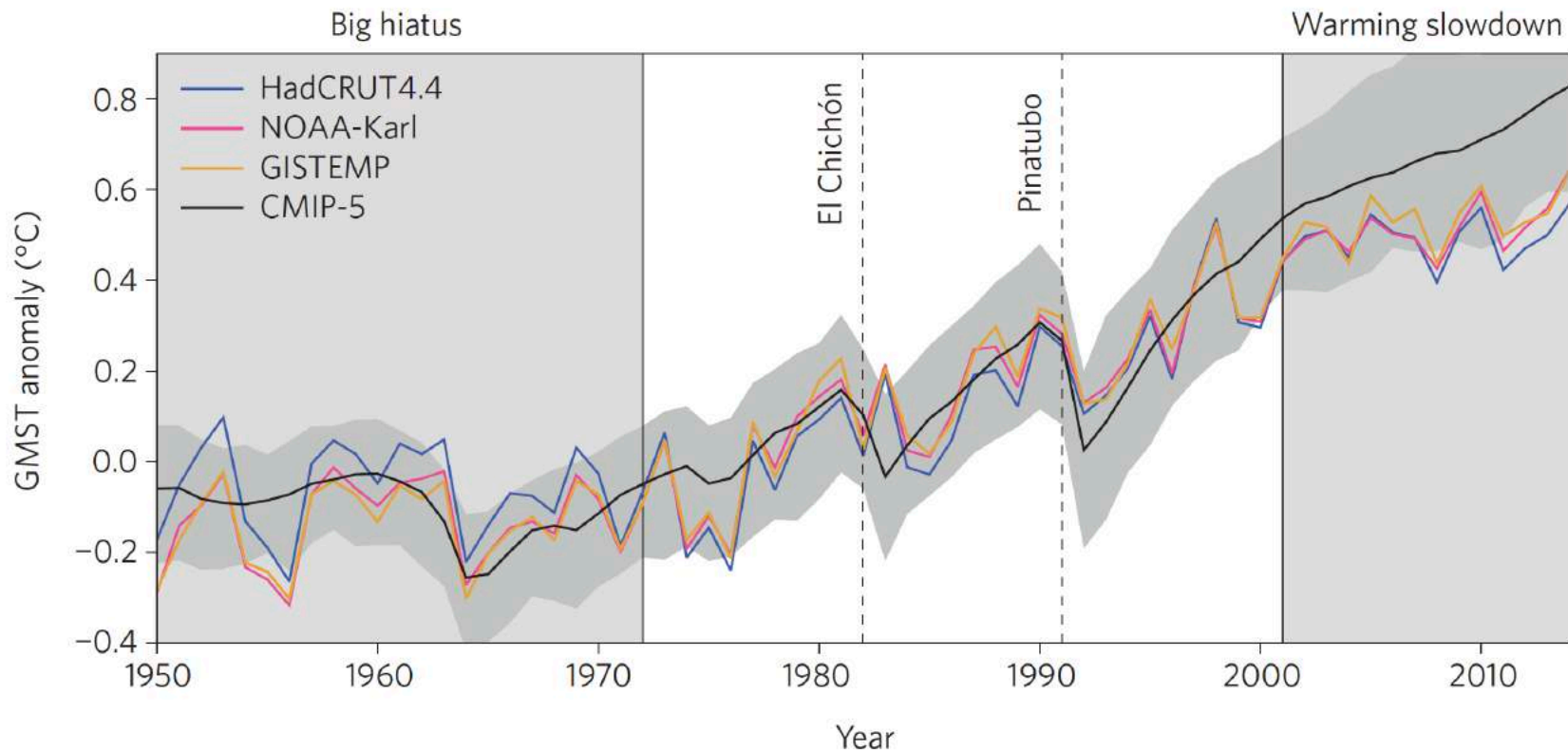
Woods Hole Oceanographic Institution, Woods Hole, MA

Estimating the Circulation and Climate of the Ocean (ECCO) Summer School
May 19-31, 2019 | Friday Harbor Laboratories | University of Washington

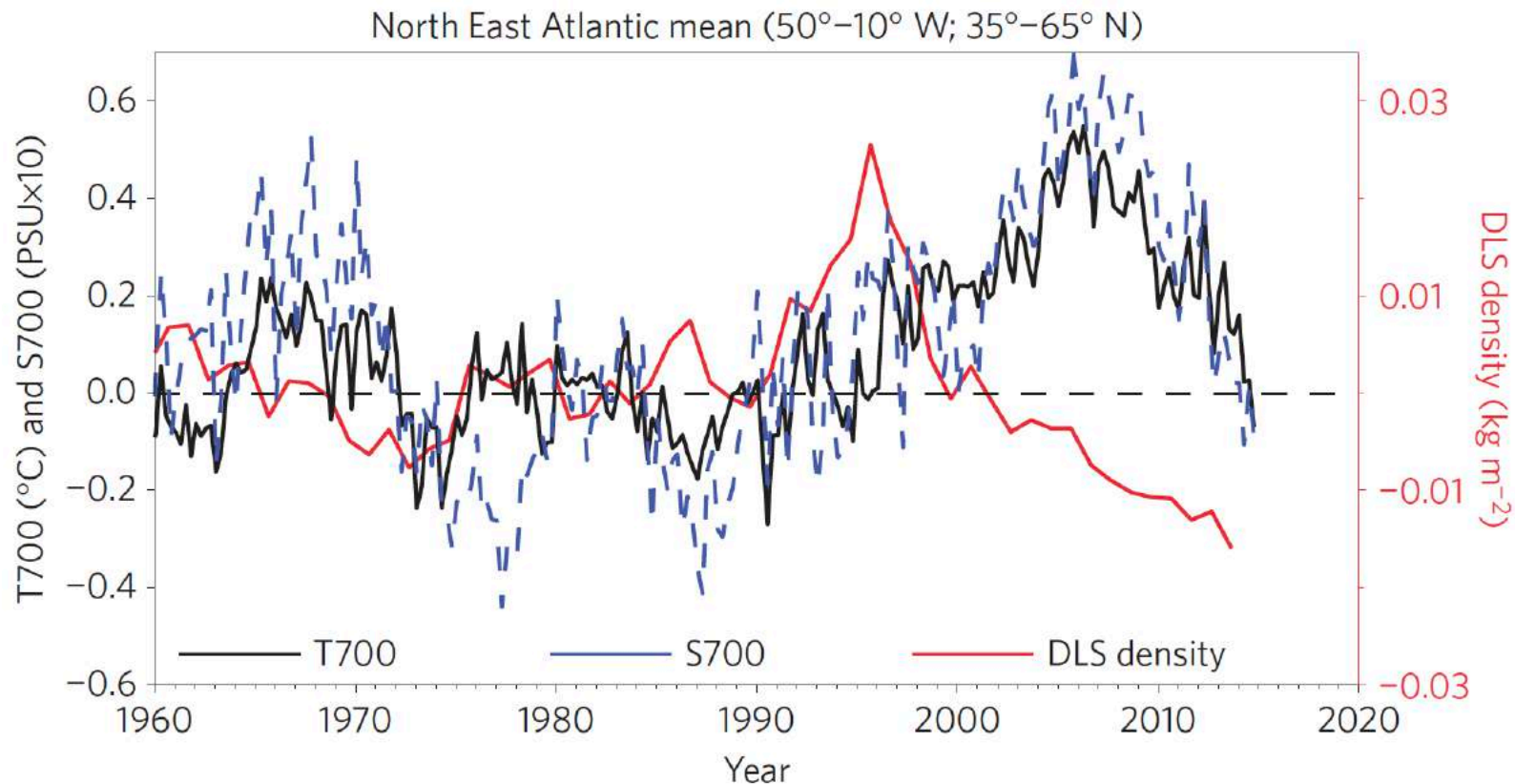


What Drives Changes in Ocean Heat & Freshwater Content?

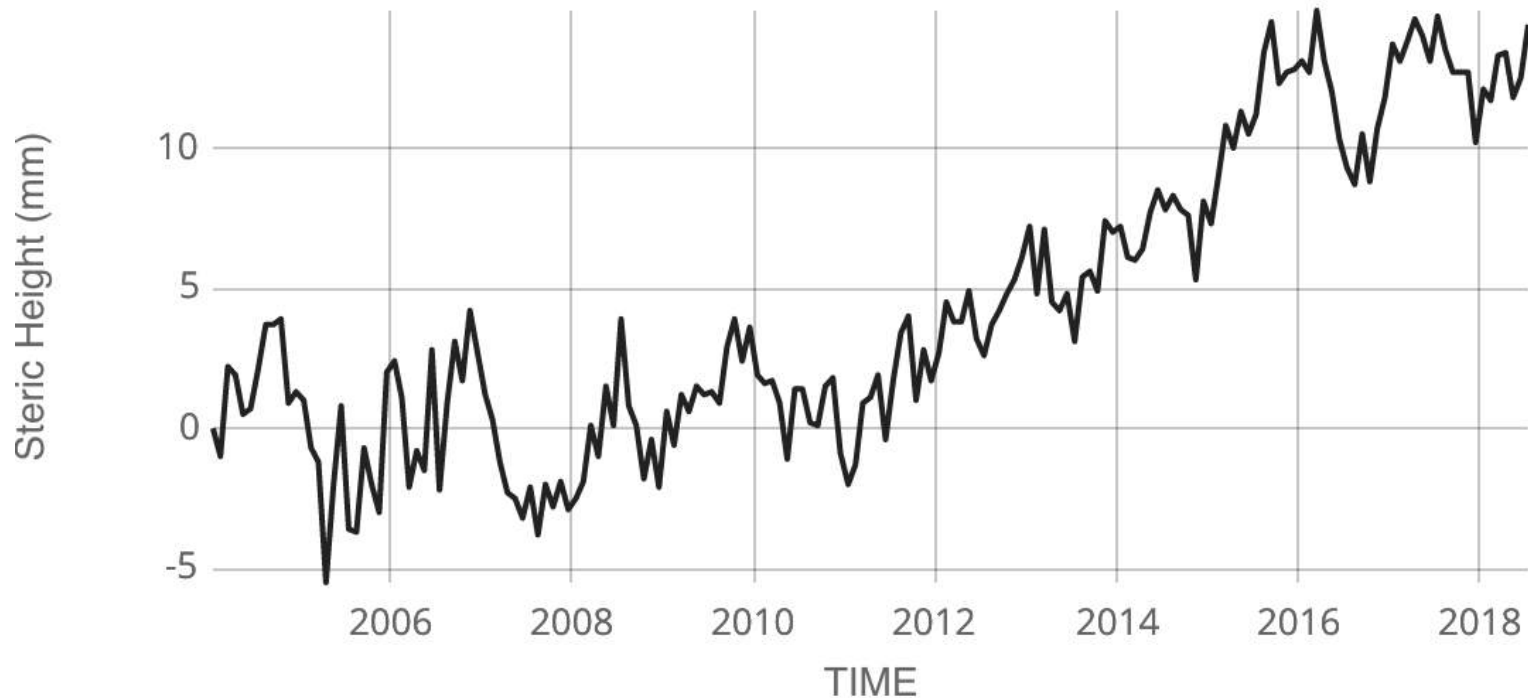
Sea-Surface Temperature & the "Slowdown"



Decadal Variability in the Subpolar North Atlantic



Ongoing Changes in Global-Mean Steric Sea Level



Roemmich and Gilson (2009), Prog. Oceanogr.
Figure provided by <https://sealevel.nasa.gov/>

Conservation Laws (in a rescaled coordinate z^*)

$$\frac{\partial (s^* \theta)}{\partial t} = -\nabla_{z^*} (s^* \theta \mathbf{v}_{res}) - \frac{\partial (\theta w_{res})}{\partial z^*} + s^* \mathcal{F}_\theta + s^* D_\theta$$

$$\frac{\partial (s^* S)}{\partial t} = -\nabla_{z^*} (s^* S \mathbf{v}_{res}) - \frac{\partial (S w_{res})}{\partial z^*} + s^* \mathcal{F}_S + s^* D_S$$

$$z^* \doteq \frac{z - \eta(x, y, t)}{H(x, y) + \eta(x, y, t)} H(x, y) \quad , \quad s^* \doteq 1 + \eta/H$$

Pop Quiz

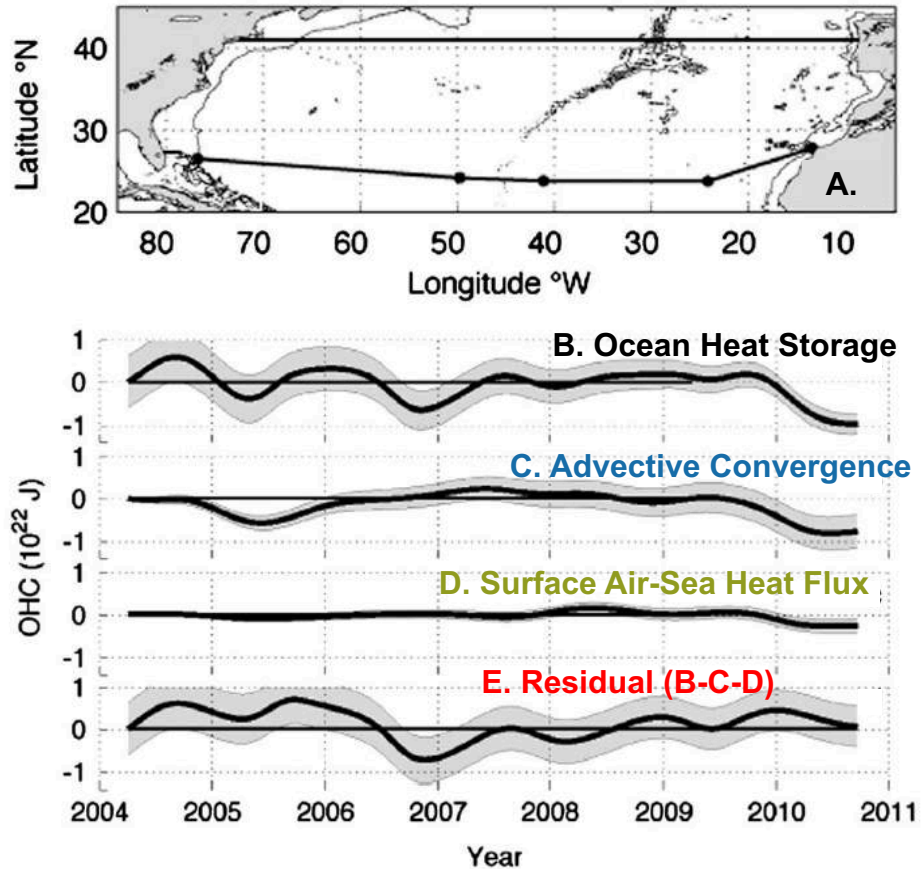
Which of the following processes can, in principle, effect changes in **globally averaged** steric sea level?

- a. Sea-surface heat exchanges
- b. Internal ocean heat advection
- c. Small-scale mixing of heat

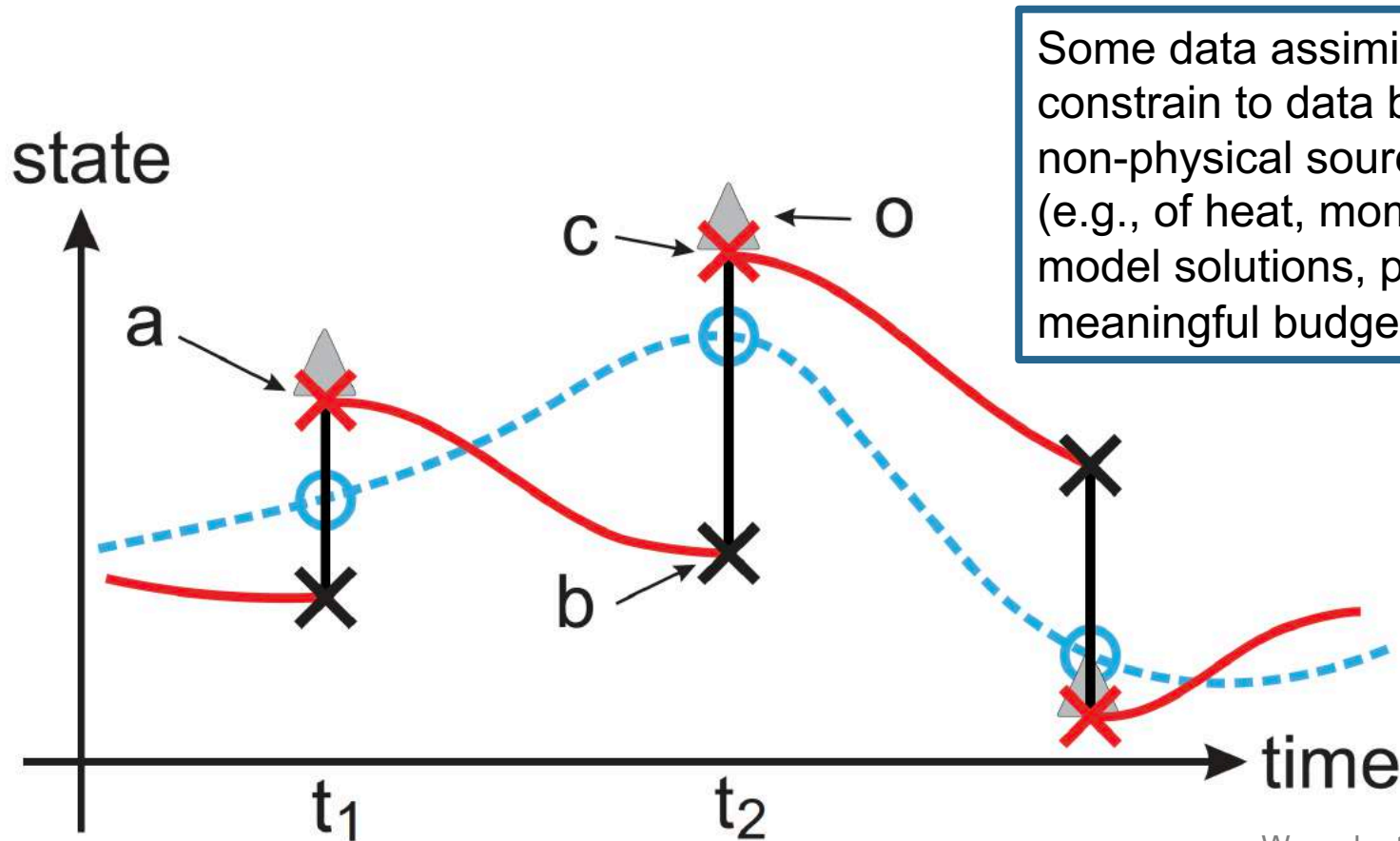
Difficulties of Closing Budgets With Ocean Data & Re-analyses

Observational Challenges

- Comprehensive diagnosis of budgets requires data that are uncertain and hard (if not impossible) to make
- Example of the 2009-2010 Subtropical North Atlantic “Cold Anomaly” (Bryden et al. 2014; Cunningham et al. 2013; Roberts et al. 201)



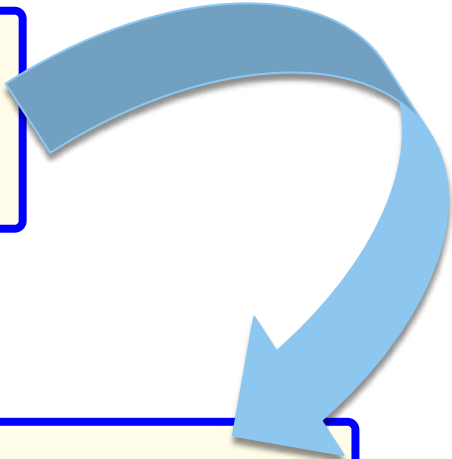
Challenges Related to Data-Assimilation Products



Some data assimilation methods constrain to data by imparting non-physical sources & sinks (e.g., of heat, momentum, etc.) to model solutions, precluding any meaningful budget analysis.

Diagnosing Budgets Using ECCO Version 4

Discretizing the Primitive Equations

$$\underbrace{\frac{\partial (s^* \theta)}{\partial t}}_{G^{\theta, tot}} = - \underbrace{\nabla_{z^*} (s^* \theta \mathbf{v}_{res}) - \frac{\partial (\theta w_{res})}{\partial z^*}}_{G^{\theta, adv}} + \underbrace{s^* \mathcal{F}_\theta}_{G^{\theta, forc}} + \underbrace{s^* D_\theta}_{G^{\theta, diff}}$$


$$\frac{s^{*n+1} \theta^{n+3/2} - s^{*n} \theta^{n+1/2}}{\Delta t} = \mathcal{A}(\theta, \mathbf{u}^{n+1} + \mathbf{u}_b^{n+1}) + s^{*n} \left(\mathcal{F}_\theta^{n+1} + D_{\sigma, \theta}^{n+1/2} + D_{\perp, \theta}^{n+3/2} \right)$$

Required MITgcm Diagnostic Output

Diagnostic	Time	Description (Units)
ETAN	Snapshot	Surface height anomaly (m)
THETA	Snapshot	Potential temperature ($^{\circ}\text{C}$)
TFLUX	Average	Total heat flux (W m^{-2})
oceQsw	Average	Net shortwave radiation (W m^{-2})
ADVr_TH	Average	Vertical advective flux of pot. temp. ($^{\circ}\text{C m}^3 \text{s}^{-1}$)
ADVx_TH	Average	Zonal advective flux of pot. temp. ($^{\circ}\text{C m}^3 \text{s}^{-1}$)
ADVy_TH	Average	Meridional advective flux of pot. temp. ($^{\circ}\text{C m}^3 \text{s}^{-1}$)
DFrI_TH	Average	Implicit vertical diffusive flux of pot. temp. ($^{\circ}\text{C m}^3 \text{s}^{-1}$)
DFrE_TH	Average	Explicit vertical diffusive flux of pot. temp. ($^{\circ}\text{C m}^3 \text{s}^{-1}$)
DFxE_TH	Average	Explicit zonal diffusive flux of pot. temp. ($^{\circ}\text{C m}^3 \text{s}^{-1}$)
DFyE_TH	Average	Explicit meridional diffusive flux of pot. temp. ($^{\circ}\text{C m}^3 \text{s}^{-1}$)

MITgcm diagnostics required to evaluate the grid-cell heat budget

Algorithm

```

1: for  $t = t_1, t_2, \dots, t_{T-1}, t_T$  do                                ▷ Loop over  $T$  time steps (months)  $t$ 
2:    $U_{i,j,k} = \text{ADVx\_TH} \{t\}$                                        ▷ 3-D average zonal advection over month  $t$ 
3:    $V_{i,j,k} = \text{ADVy\_TH} \{t\}$                                        ▷ 3-D average meridional advection over month  $t$ 
4:    $W_{i,j,k} = \text{ADVr\_TH} \{t\}$                                        ▷ 3-D average vertical advection over month  $t$ 
5:    $\mathcal{U}_{i,j,k} = \text{DFxE\_TH} \{t\}$                                    ▷ 3-D average zonal diffusion over month  $t$ 
6:    $\mathcal{V}_{i,j,k} = \text{DFyE\_TH} \{t\}$                                    ▷ 3-D average meridional diffusion over month  $t$ 
7:    $\mathcal{W}_{i,j,k}^E = \text{DFyE\_TH} \{t\}$                                    ▷ 3-D average vertical diffusion (explicit) over month  $t$ 
8:    $\mathcal{W}_{i,j,k}^I = \text{DFyI\_TH} \{t\}$                                    ▷ 3-D average vertical diffusion (implicit) over month  $t$ 
9:    $N_{i,j}^{(0)} = \text{ETAN} \{t - \Delta t\}$                                ▷ 2-D surface height snapshot at start of month  $t$ 
10:   $N_{i,j}^{(f)} = \text{ETAN} \{t\}$                                          ▷ 2-D surface height snapshot at end of month  $t$ 
11:   $T_{i,j,k}^{(0)} = \text{THETA} \{t - \Delta t\}$                              ▷ 3-D temperature snapshot at start of month  $t$ 
12:   $T_{i,j,k}^{(f)} = \text{THETA} \{t\}$                                        ▷ 3-D temperature snapshot at end of month  $t$ 
13:   $v_{i,j,k} = h_{i,j,k} A_{i,j} \Delta z_k$                                ▷ Grid volume

```

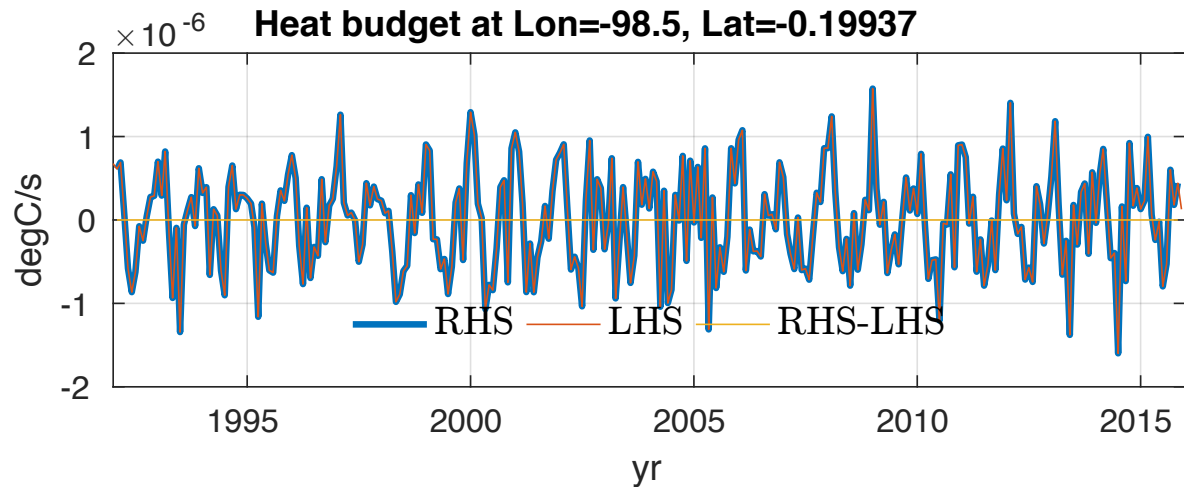
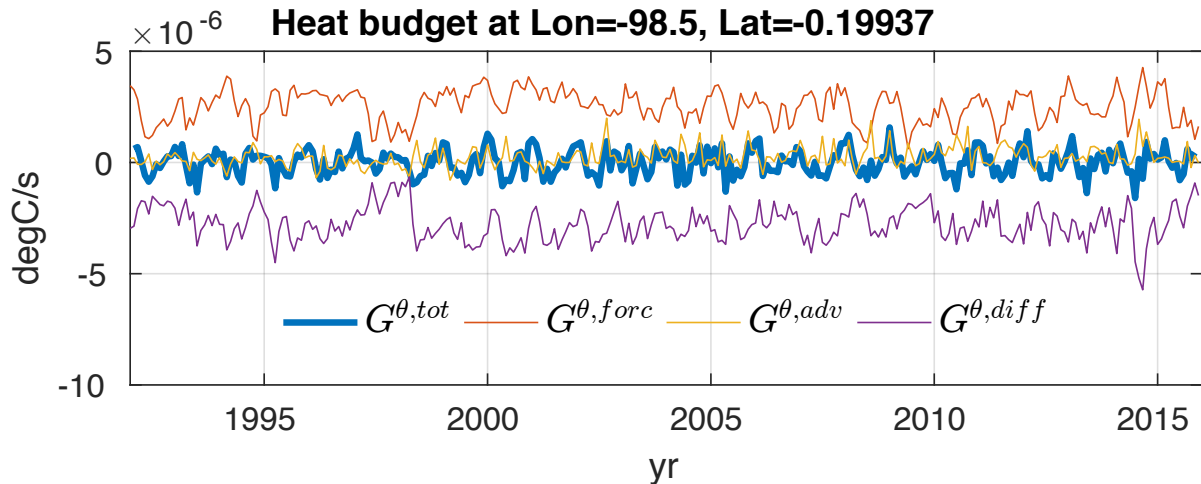
Algorithm

```

14:   for  $i = i_1, i_2, \dots, i_{I-1}, i_I$  do                                ▷ Loop over  $I$  longitude cells  $i$ 
15:       for  $j = j_1, j_2, \dots, j_{J-1}, j_J$  do                            ▷ Loop over  $J$  latitude cells  $j$ 
16:            $s_{i,j}^{*(0)} = \left( 1 + N_{i,j}^{(0)} / H_{i,j} \right)$ 
17:            $s_{i,j}^{*(f)} = \left( 1 + N_{i,j}^{(f)} / H_{i,j} \right)$ 
18:           for  $k = k_1, k_2, \dots, k_{K-1}, k_K$  do                        ▷ Loop over  $K$  vertical cells  $k$ 
19:                $G_{i,j,k}^{\theta,tot} = \left( T_{i,j,k}^{(f)} s_{i,j}^{*(f)} - T_{i,j,k}^{(0)} s_{i,j}^{*(0)} \right) / \Delta t$ 
20:                $G_{i,j,k}^{\theta,advH} = (U_{i,j,k} - U_{i+1,j,k} + V_{i,j,k} - V_{i,j+1,k}) / v_{i,j,k}$ 
21:                $G_{i,j,k}^{\theta,diffH} = (\mathcal{U}_{i,j,k} - \mathcal{U}_{i+1,j,k} + \mathcal{V}_{i,j,k} - \mathcal{V}_{i,j+1,k}) / v_{i,j,k}$ 
22:                $G_{i,j,k}^{\theta,advV} = [(1 - \delta_{k,K}) W_{i,j,k+1} - W_{i,j,k}] / v_{i,j,k}$ 
23:                $G_{i,j,k}^{\theta,diffV} = [(1 - \delta_{k,K}) (\mathcal{W}_{i,j,k+1}^E + \mathcal{W}_{i,j,k+1}^I) - \mathcal{W}_{i,j,k}^E - \mathcal{W}_{i,j,k}^I] / v_{i,j,k}$ 
24:                $G_{i,j,k}^{\theta,adv} = G_{i,j,k}^{\theta,advH} + G_{i,j,k}^{\theta,advV}$ 
25:                $G_{i,j,k}^{\theta,diff} = G_{i,j,k}^{\theta,diffH} + G_{i,j,k}^{\theta,diffV}$ 
26:           end for
27:       end for
28:   end for

```

Example of Closure



A Practical Guide

- For more details, come to tomorrow's tutorial and "hands-on" lab session—
 - ▣ Friday, May 24th
 - ▣ 3:00-4:00 PM; 4:30-6:30 PM

- A full guide is available and downloadable—
 - ▣ <https://dspace.mit.edu/handle/1721.1/111094>

A Note on Practical Evaluation of Budgets in ECCO Version 4 Release 3

Christopher G. Piecuch (cpiecuch@aer.com)

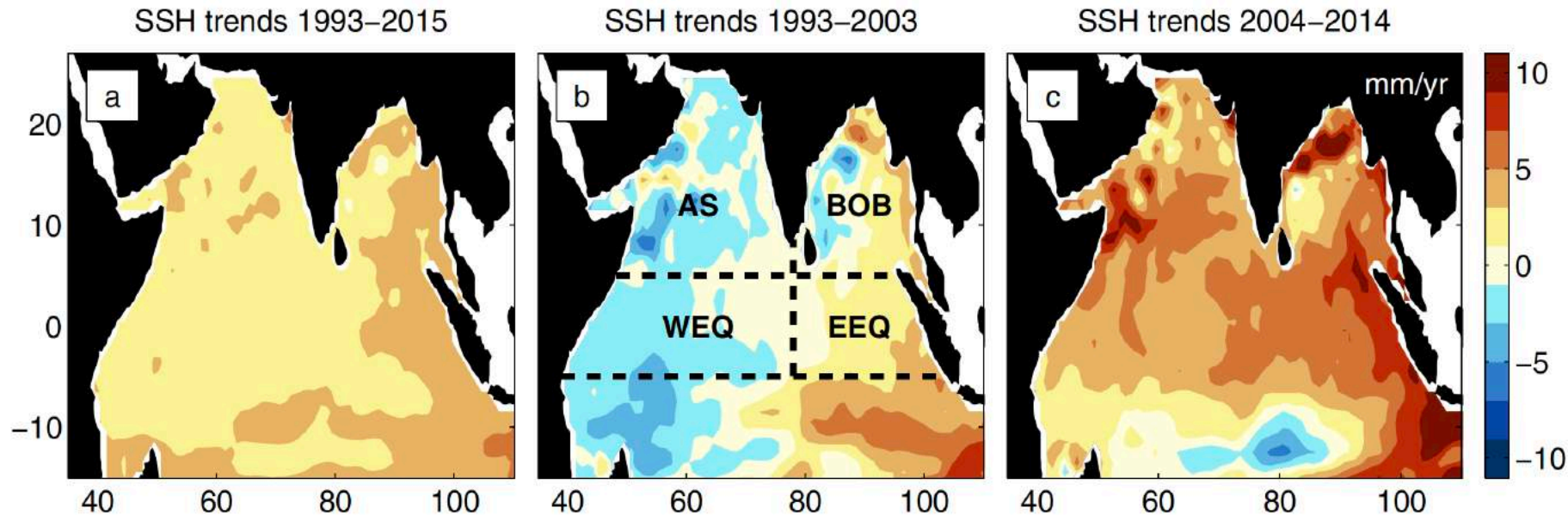
June 16, 2017

Contents	1
1 Introduction	2
1.1 Scope	2
2 Obtaining ECCOv4 Release 3	3
3 Model Configuration	3
4 Budgets Evaluated for Extensive Quantities	5
4.1 Volume Conservation	5
4.2 Heat Conservation	7
4.2.1 Geothermal Flux	10
4.3 Salt Conservation	12
5 Budgets Estimated for Intensive Quantities	16
5.1 Salinity Budget	16
A Example Matlab Code and the gcmfaces Framework	18
A.1 The gcmfaces Framework	18
A.2 Example Matlab code	19

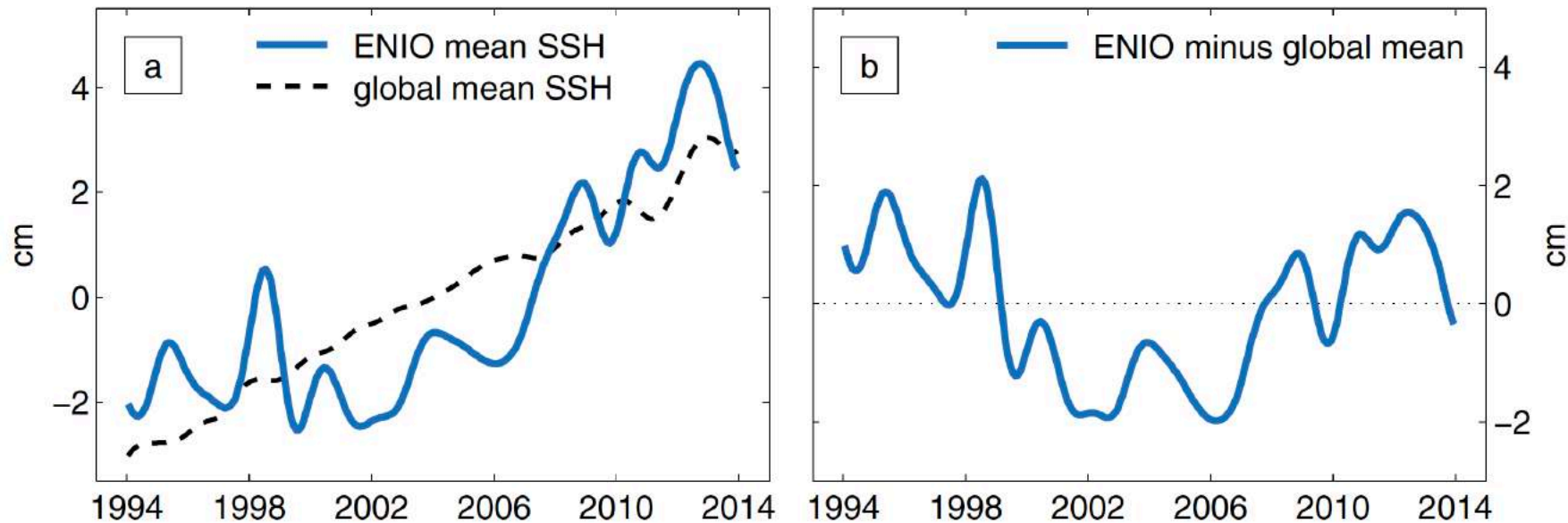
A Few Illustrative Vignettes

**Vignette #1—
Sea Level & Heat Content in the
Tropical Indian Ocean**

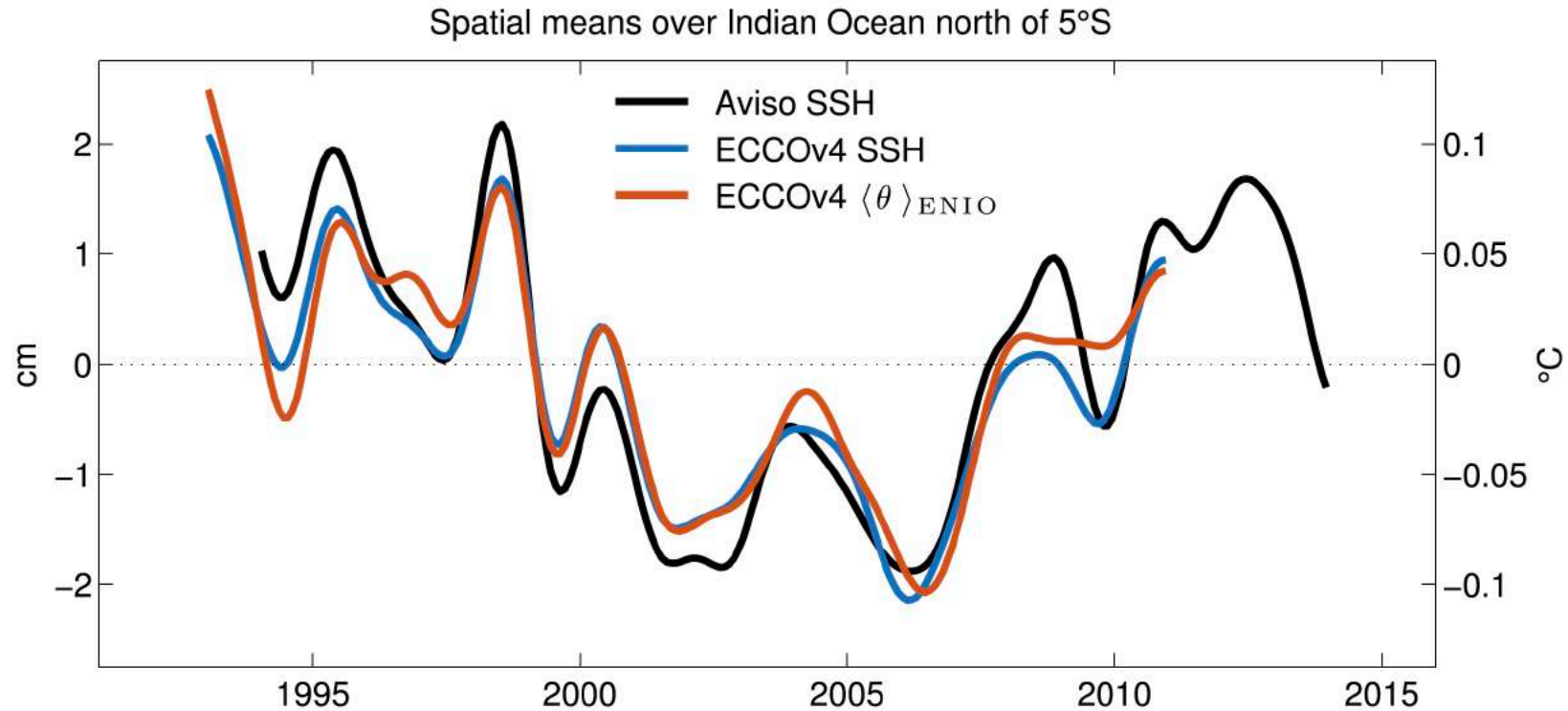
Sea Level & Heat Content in the Tropical Indian



Sea Level & Heat Content in the Tropical Indian

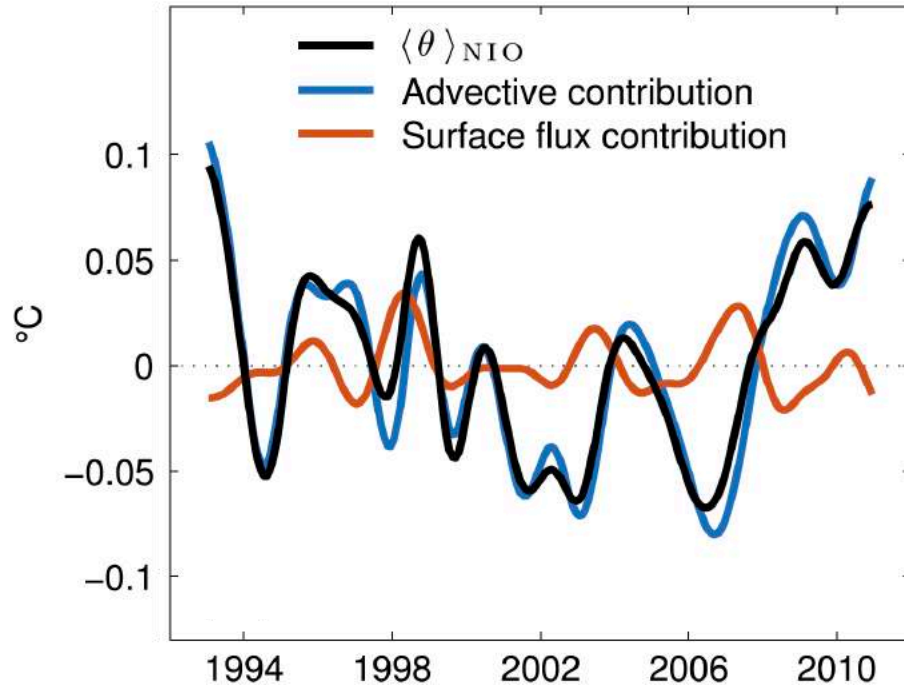


Sea Level & Heat Content in the Tropical Indian

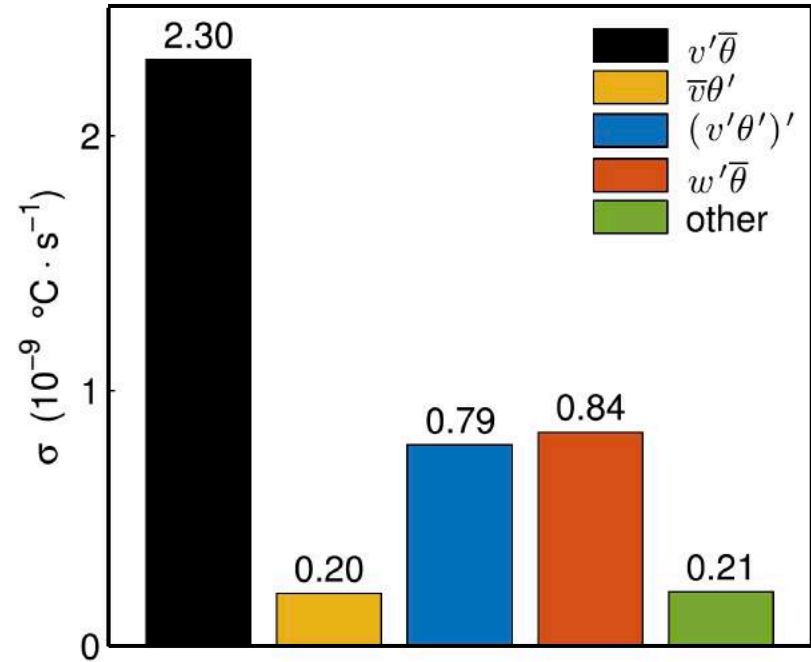


Sea Level & Heat Content in the Tropical Indian

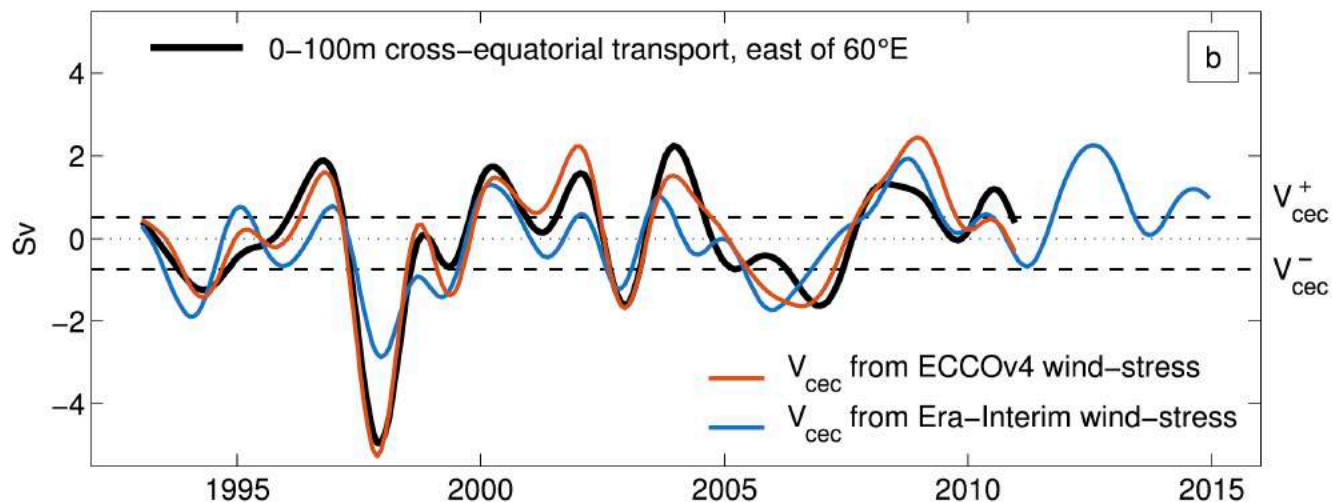
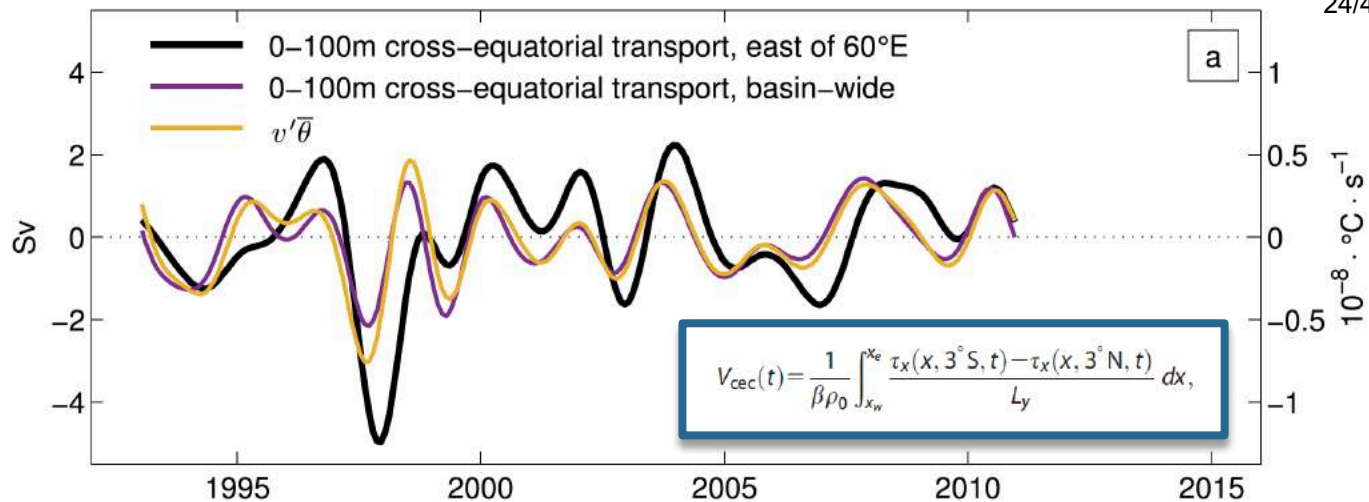
A. Time Series of Major Budget Terms



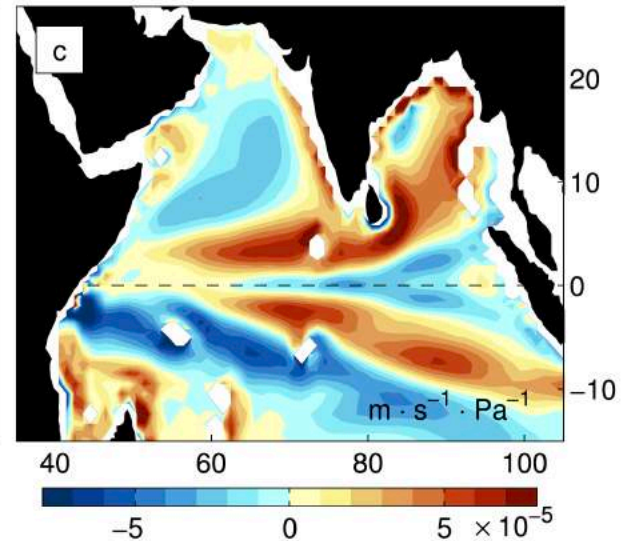
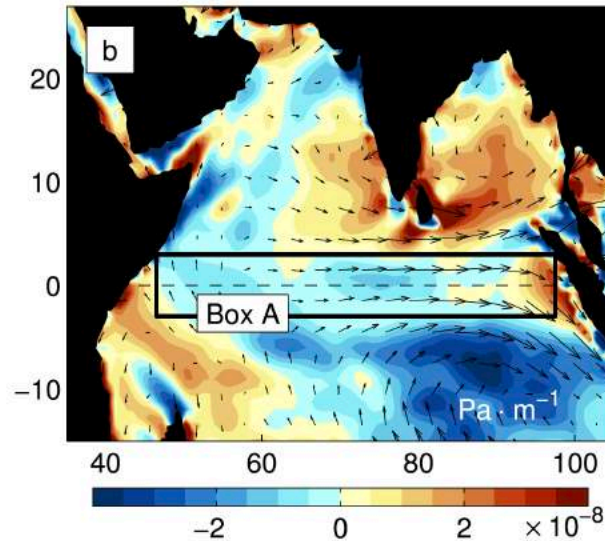
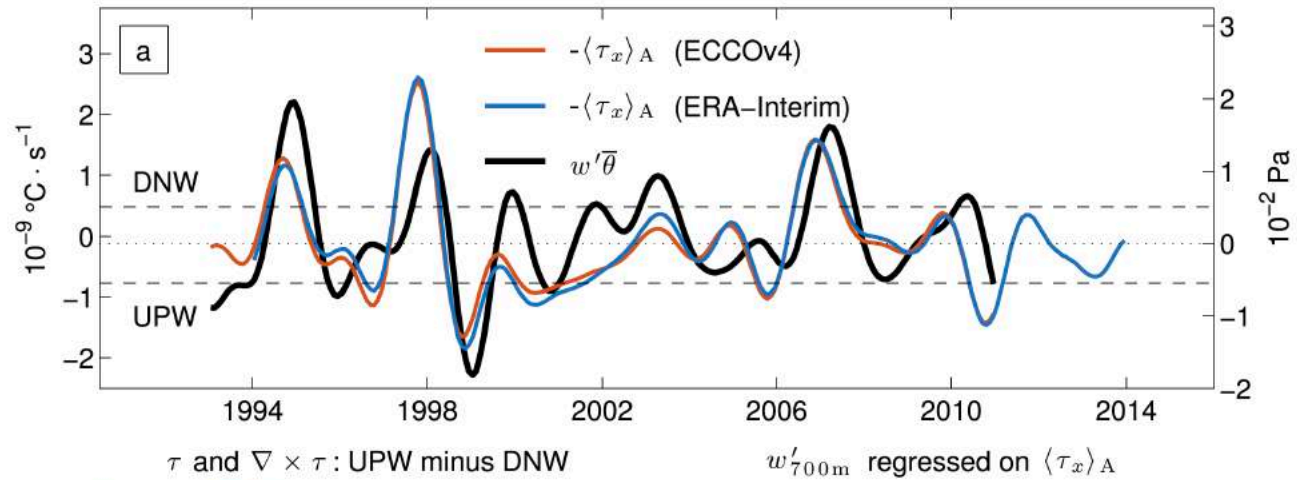
B. Std. Dev. of Advection Terms



Sea Level & Heat Content in the Tropical Indian

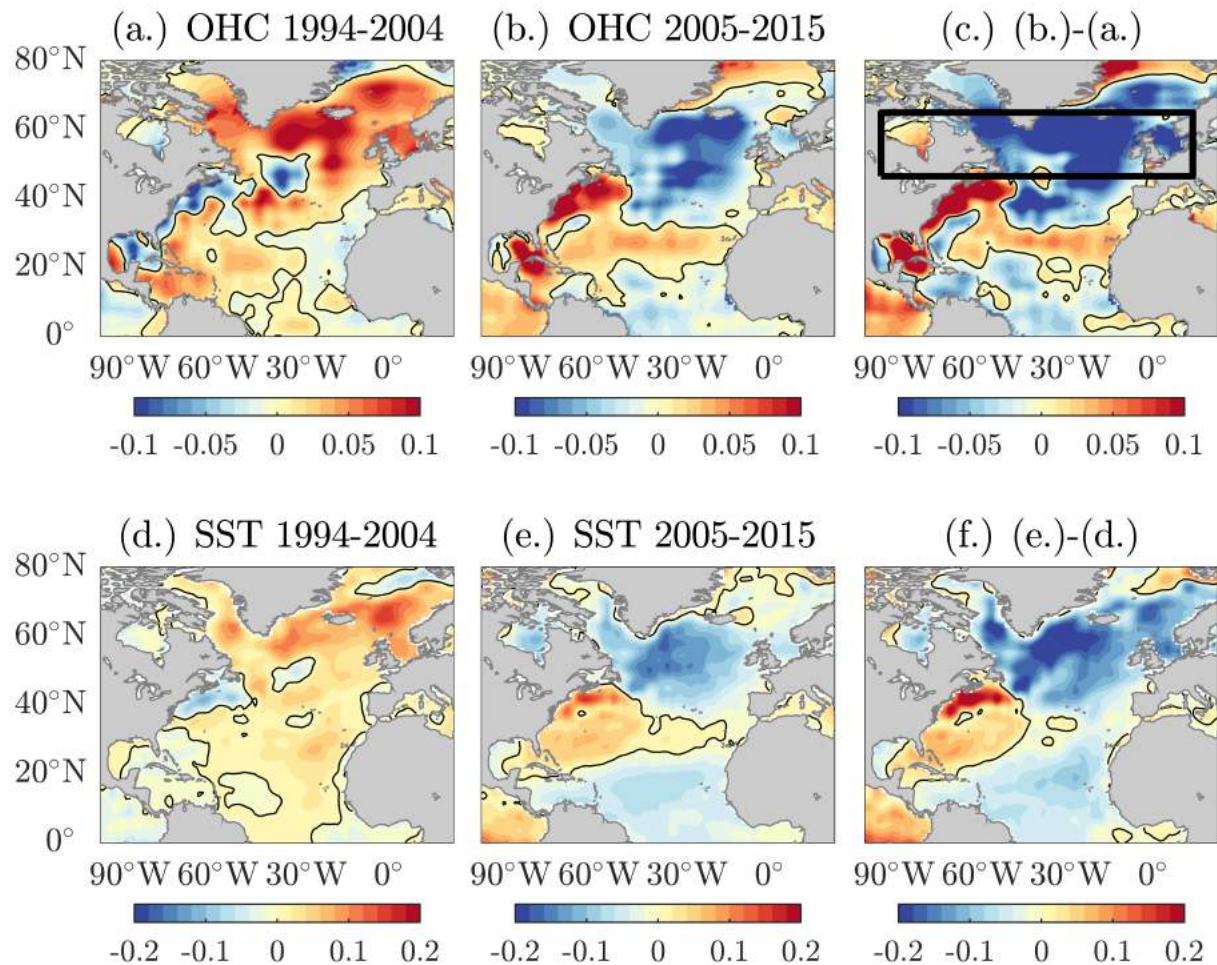


Sea Level & Heat Content in the Tropical Indian

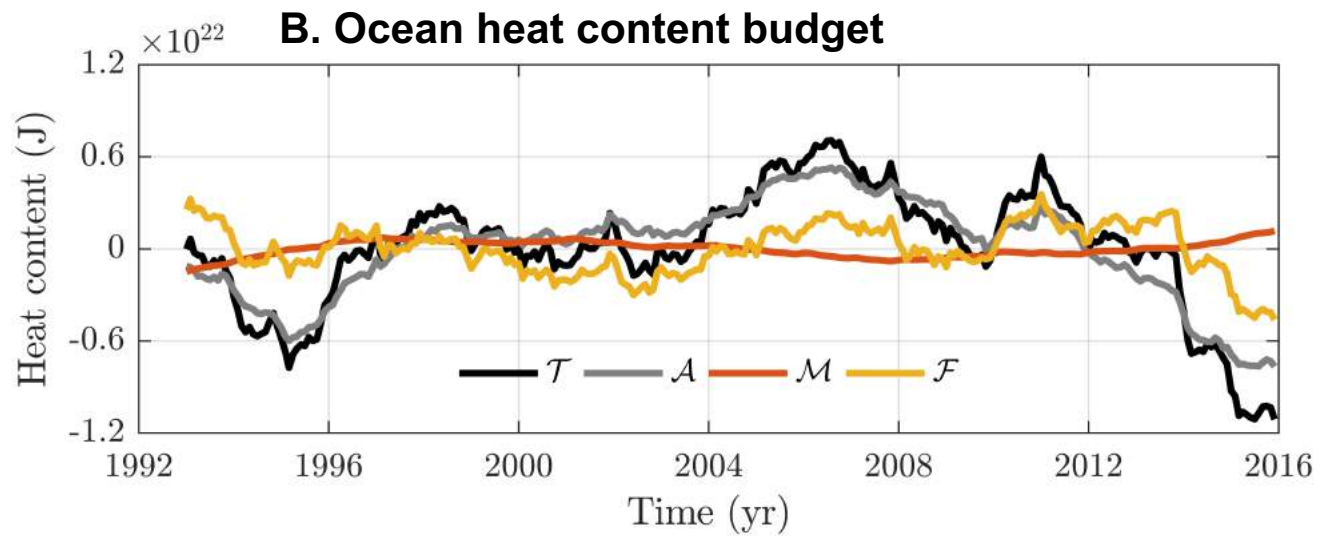
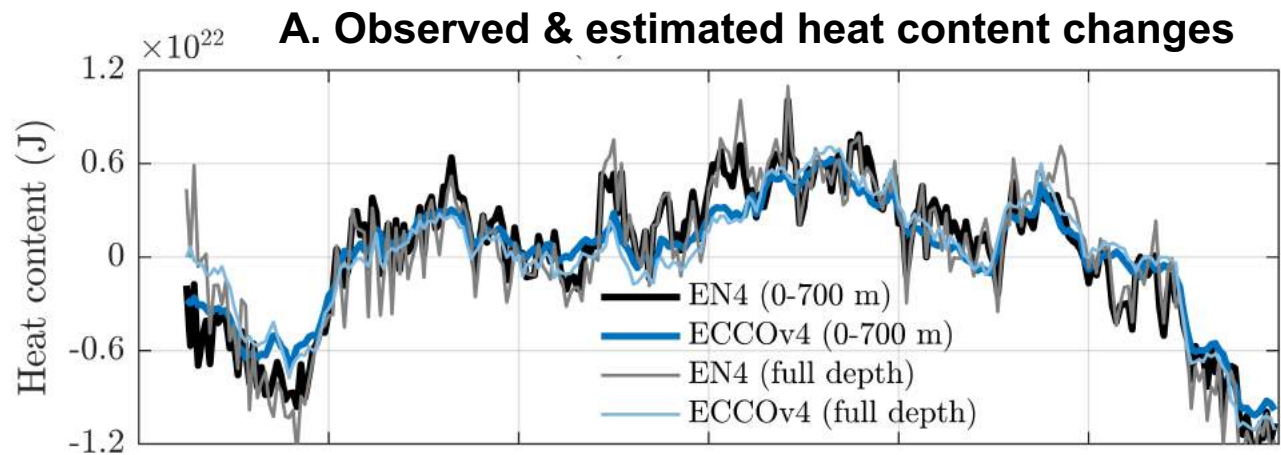


**Vignette #2—
Decadal Variability in the
Subpolar North Atlantic Ocean**

Regional Heat Content in the North Atlantic

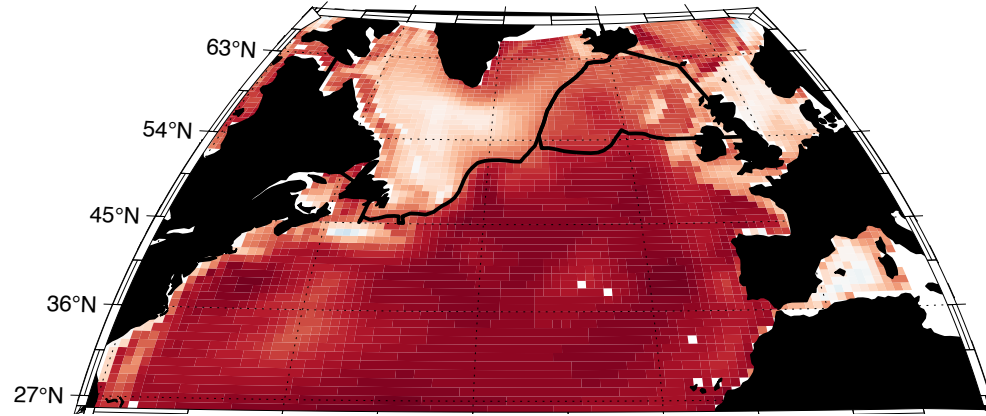


Regional Heat Content in the North Atlantic

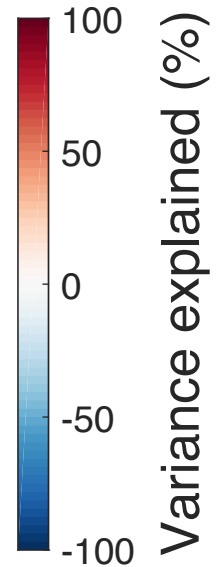
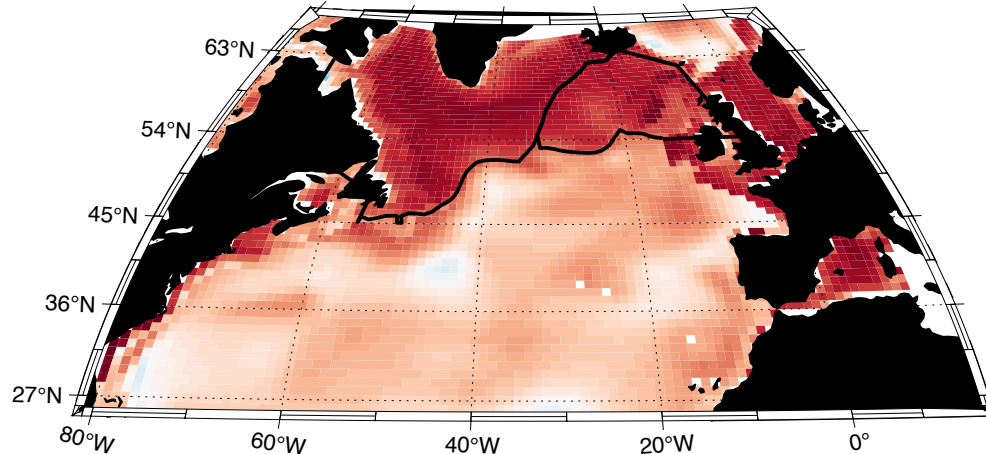


Regional Heat Content in the North Atlantic

A. OHC variance due to wind stress

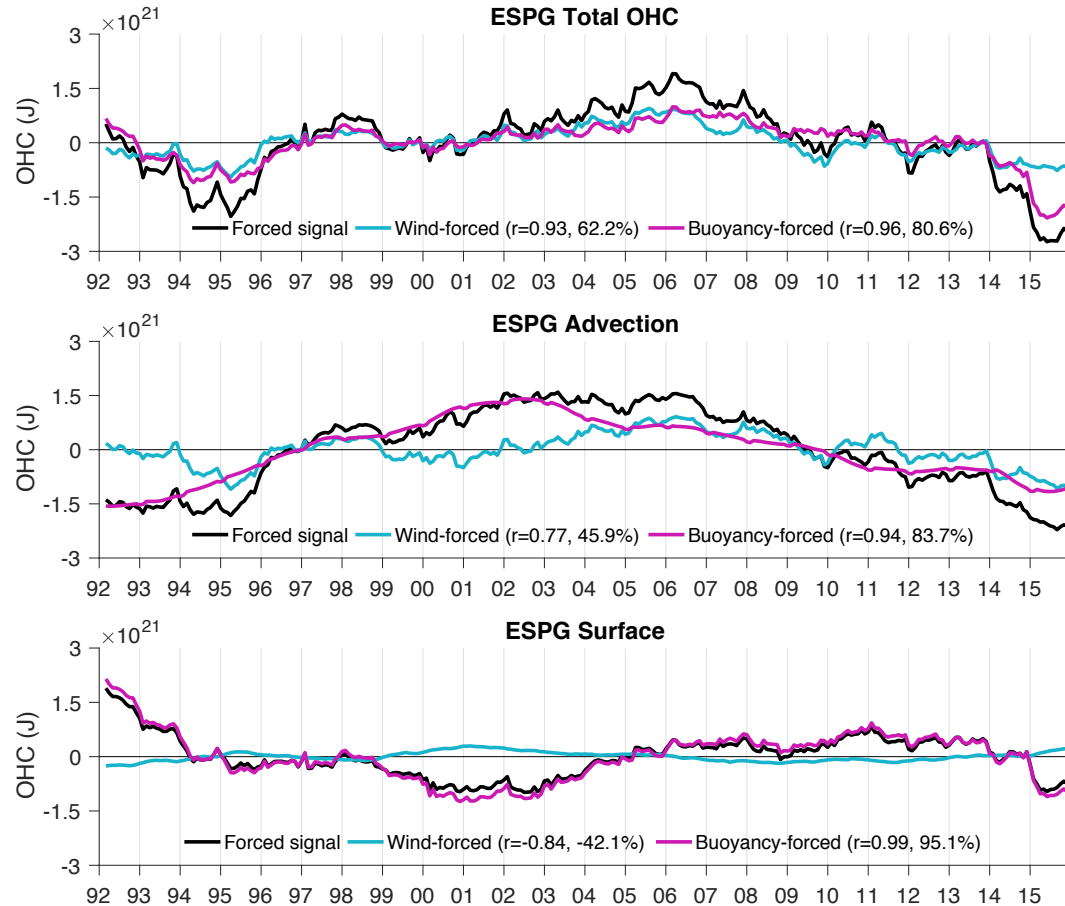


B. OHC variance due to buoyancy flux



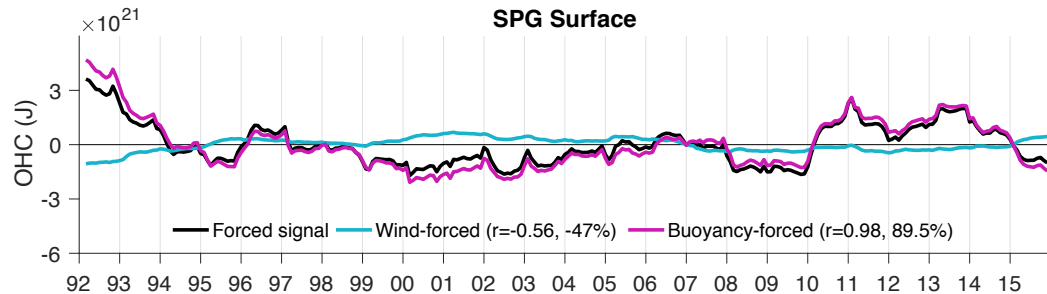
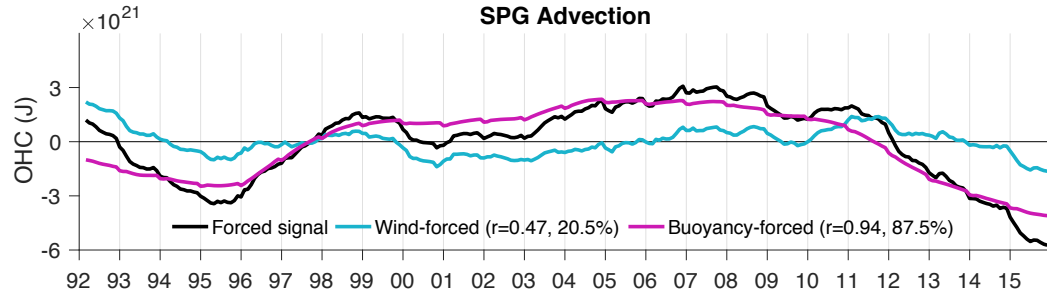
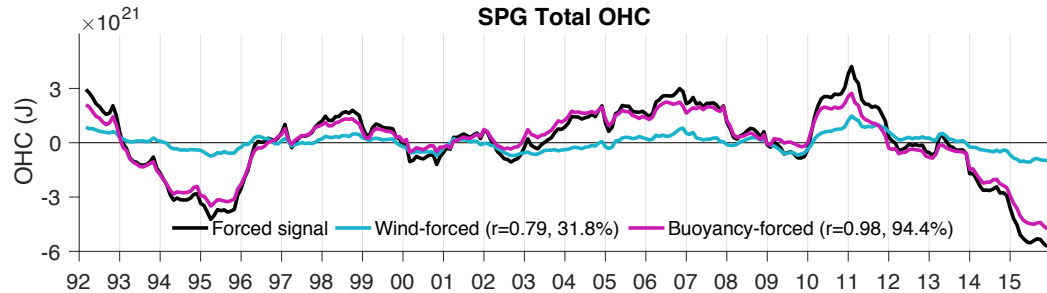
Regional Heat Content in the North Atlantic

Forcing of Eastern Subpolar Gyre Budget



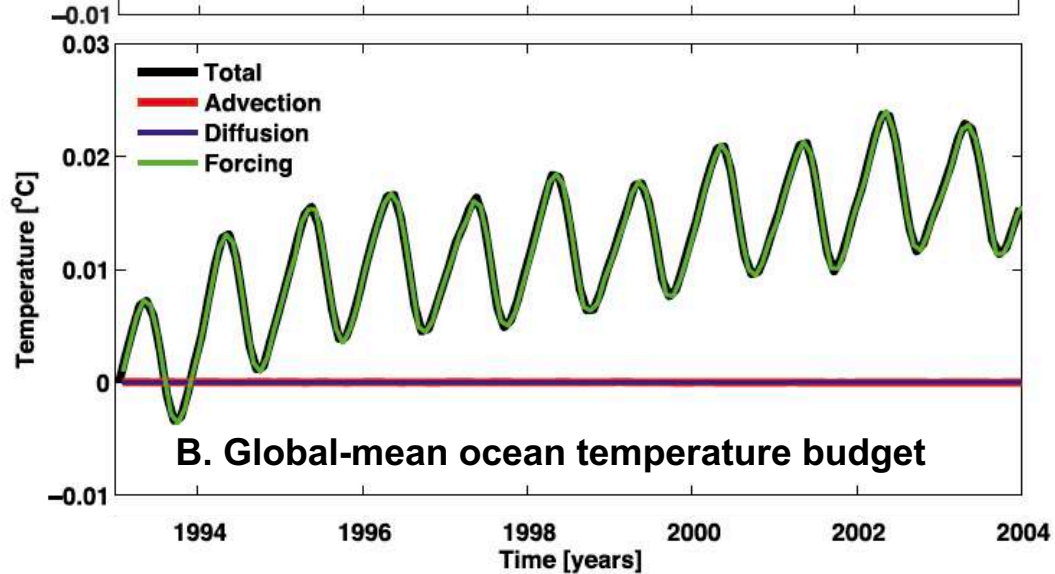
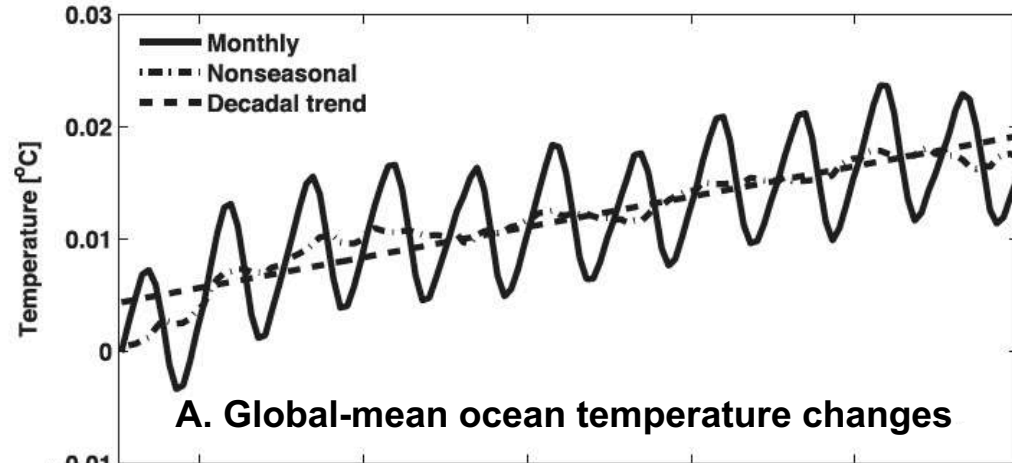
Forcing of Subpolar Gyre/Labrador Sea Budget

Regional Heat Content in the North Atlantic

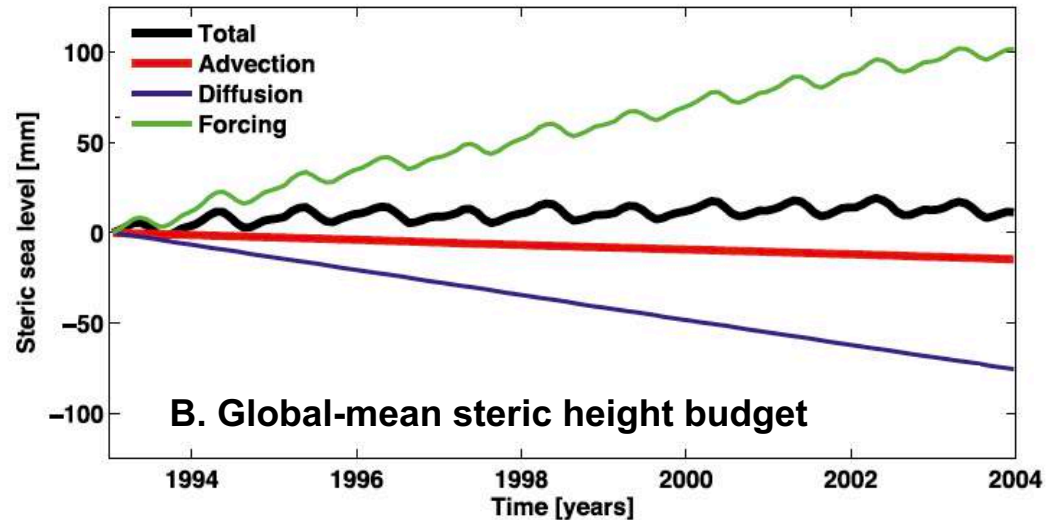
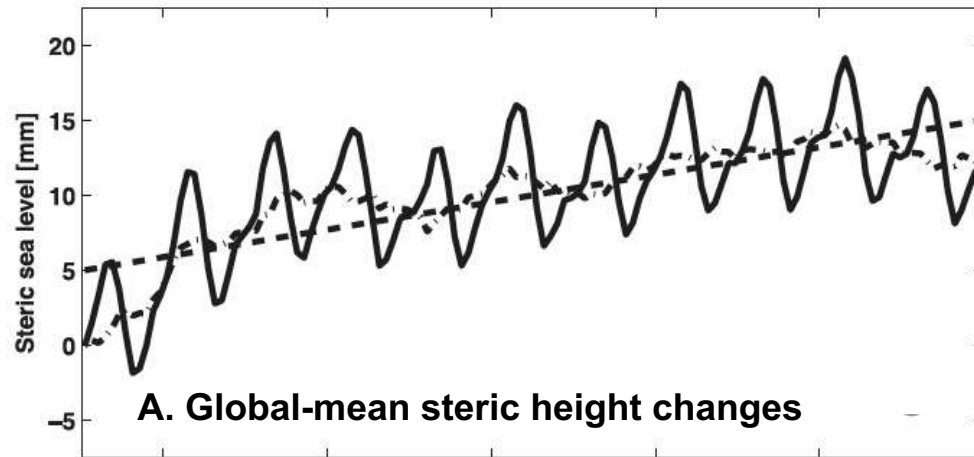


**Vignette #3—
Global-Mean Steric
Sea Level Change**

Global-Mean Steric Sea Level



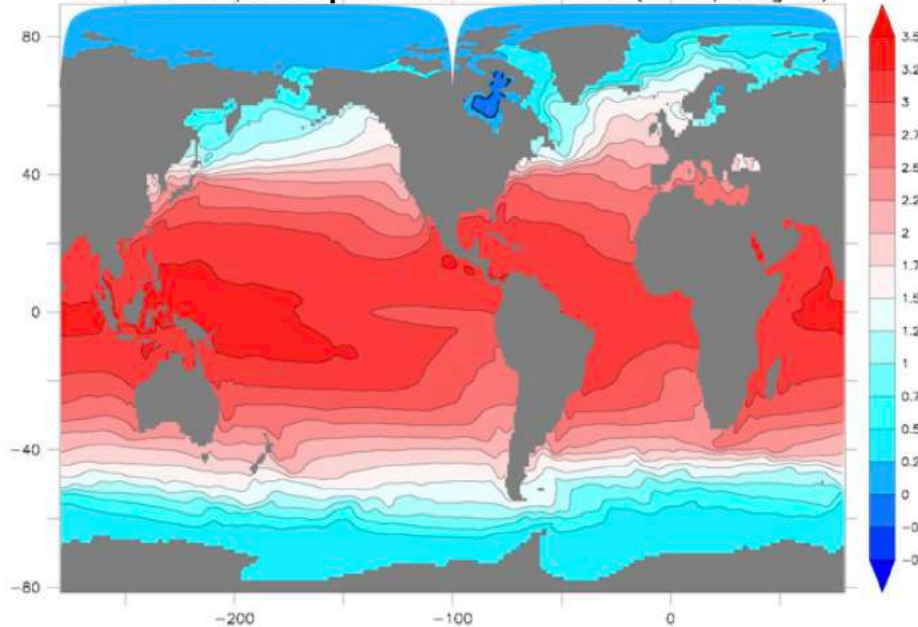
Global-Mean Steric Sea Level



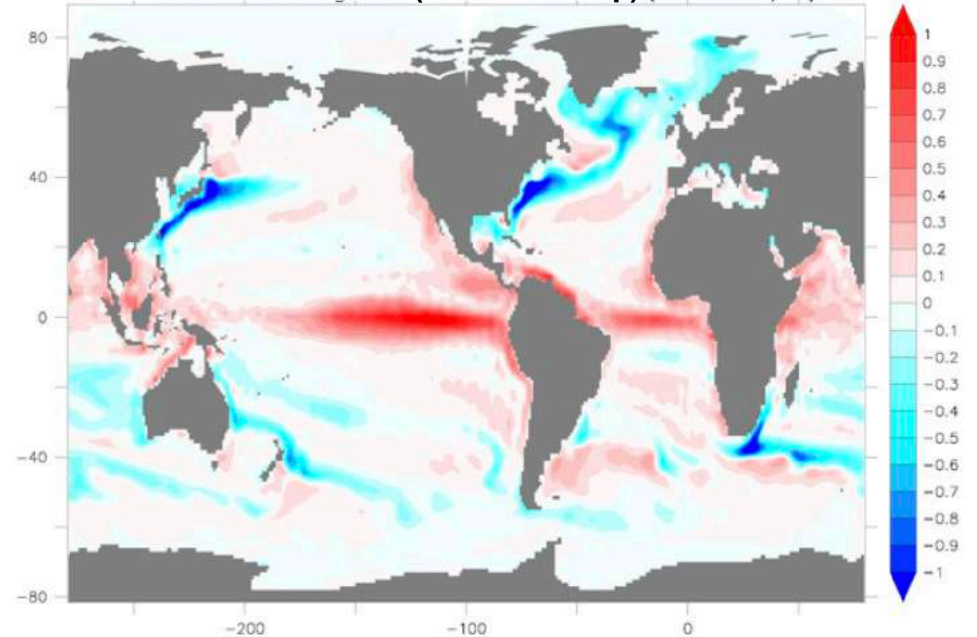
Global-Mean Steric Sea Level

Nonlinear Equation of State Effects

A. Thermal Expansion Coefficient ($\times 10^4 / \text{deg C}$)

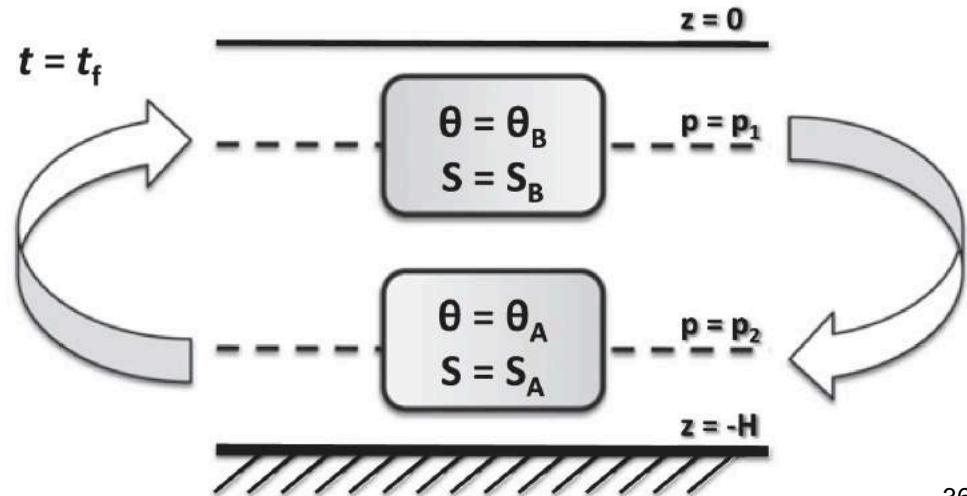
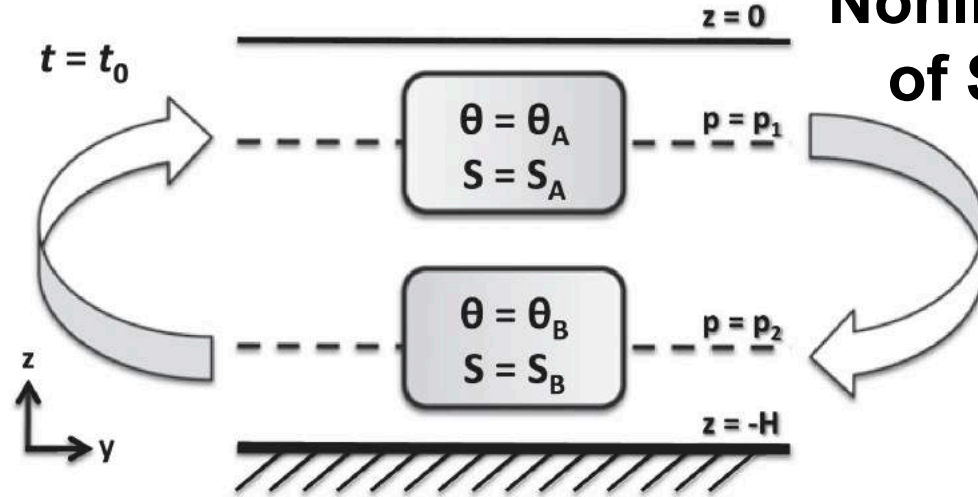


B. Surface Heat Flux (Sea Level Eq.) ($\times 10^8 \text{ m/s}$)



Global-Mean Steric Sea Level

Nonlinear Equation of State Effects



Time is Always Against Us ...

- Other examples (that sadly I don't have time to discuss)
 - Heat budgets—Kim et al. (2004, 2007); Lee et al. (2004); Nie et al. (2013); Buckley et al. (2014); Tamsitt et al. (2016); Ponte & Piecuch (2018); Su et al. (2018); Asbjørnsen et al. (2019) ...
 - Salt & salinity budgets—Qu et al. (2011, 2013); Vinogradova & Ponte (2013, 2017); Gao et al. (2014) Ponte & Vinogradova (2017) ...
 - Regional steric height budgets—Piecuch & Ponte (2011, 2012, 2013) ...
 - Momentum budgets—Sonnewald et al. (2019) ...
 - ...

Oh, Right ... Pop Quiz

Which of the following processes can, in principle, effect changes in **globally averaged** steric sea level?

- a. Sea-surface heat exchanges
- b. Internal ocean heat advection
- c. Small-scale mixing of heat

Oh, Right ... Pop Quiz

Which of the following processes can, in principle, effect changes in **globally averaged** steric sea level?

- a. **Sea-surface heat exchanges**
- b. **Internal ocean heat advection**
- c. **Small-scale mixing of heat**

Summary

- Budget analysis is a powerful tool for understanding and identifying the mechanisms of oceanic change
- Difficulties with observations often preclude closed budget analyses
- The data-constrained and physically consistent nature of the ECCO state estimates allows for meaningful budget attribution of observed oceanic changes

Thank you.

